Stat 852 Fall 2011 Assignment #3

This assignment is due at the beginning of class on Wednesday, November 2, 2011.

**1.** Recall question 6 on Assignment #2. Let  $X_1, X_2, \ldots, X_n$  be iid with the geometric distribution

$$P_{\theta}(X=x) = \theta(1-\theta)^{x-1}, \quad x=1,2,\ldots, \quad 0 < \theta < 1.$$

Show that

$$\sum_{i=1}^{n} X_i$$

is sufficient for  $\theta$  and find the family of distributions of this statistic. Is the family complete?

- **2.** Exercise 6.18 page 302
- **3.** Exercise 6.19 page 302
- **4.** Exercise 7.1 page 355
- **5.** Exercise 7.6 page 355
- **6.** Exercise 7.7 page 355
- **7.** Exercise 7.22 page 358
- 8. Exercise 7.24 page 359
- **9.** Let  $X_1$  and  $X_2$  be iid random variables with density function given by

$$f(x|\theta) = \theta e^{-\theta x} I(x > 0)$$

for  $\theta \in \Theta = (0, \infty)$ .

- (a) Is the family of distributions of  $(X_1, X_2)$  an exponential family? Justify your answer.
- (b) Use Basu's Theorem to show that  $X_1 + X_2$  and  $X_1/X_2$  are independent for all  $\theta \in \Theta$ .
- **10.** Exercise 6.21 (a) and (b) page 302
- **11.** Exercise 6.40 page 306