Stat 252 Winter 2007
Assignment \#6

This assignment is due at the beginning of class on Monday, March 5, 2007. You must submit all problems that are marked with an asterix (*).

1.     * Do the following exercises from Wackerly, et al.

- \#9.73, page 453
- \#9.74 (b), page 453
- \#9.75 (a), page 453
- \#9.76, page 453
- \#9.77 (a), page 454

2.     * A biologist is studying an animal population of unknown size. For each of five consecutive days, she sets a (big) trap in the morning. In the evening, she counts how many animals wandered into her trap, before releasing them. She would like to estimate both $p$, the probability that any particular animal will be trapped in any particular day, and $k$, the total size of the population.
(a) Let $Y_{i}$ denote the number of animals trapped on day $i$. The biologist postulates that $Y_{1}, \ldots, Y_{n}$ are independent and identically distributed as $\operatorname{Bin}(k, p)$. Comment very briefly on whether or not you think this is reasonable.
(b) Assume that data $y_{1}=13, y_{2}=15, y_{3}=14, y_{4}=9, y_{5}=12$ are observed. Determine the method of moments estimates for $k$ and $p$.
(c) What if $y_{5}=5$ had been observed, instead of $y_{5}=12$. Recompute your estimates. Do you have any comments?
(Note: This is an uncommon use of the $\operatorname{Bin}(k, p)$ distribution. Experiments where $k$ is known (fixed by the experimenter) and only $p$ is unknown are much more common.)
