

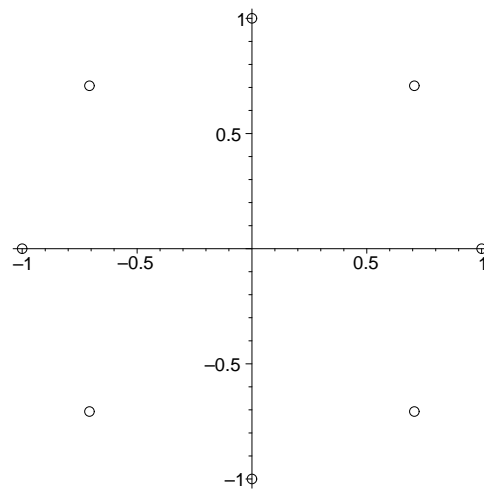
Math 103.01 Summer 2001  
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**Example:** Determine the graph of the curve  $x = \cos t$ ,  $y = \sin t$  for  $0 \leq t \leq 2\pi$ .

We begin by plotting a few points.

$t$	$(x, y)$
0	(1, 0)
$\pi/4$	$(1/\sqrt{2}, 1/\sqrt{2})$
$\pi/2$	(0, 1)
$3\pi/4$	$(-1/\sqrt{2}, 1/\sqrt{2})$
$\pi$	(-1, 0)
$5\pi/4$	$(-1/\sqrt{2}, -1/\sqrt{2})$
$3\pi/2$	(0, -1)
$7\pi/4$	$(1/\sqrt{2}, -1/\sqrt{2})$
$2\pi$	(1, 0)

Plotting these points suggest that  $(x, y)$  lie in a circle.



Note that  $x^2 + y^2 = \cos^2 t + \sin^2 t = 1$  for all  $t$ .

Therefore,  $x = \cos t$ ,  $y = \sin t$ , for  $0 \leq t \leq 2\pi$  describes the unit circle in  $\mathbb{R}^2$ .