Math 111.01 Summer 2003 In Class Exercise (June 27, 2003)

**Example:** Exercise #1 on page 99. A tank holds 1000 gal of water which drains from the bottom in 30 minutes

| after $t \min$    | 5   | 10  | 15  | 20  | 25 | 30 |
|-------------------|-----|-----|-----|-----|----|----|
| vol $V$ remaining | 694 | 444 | 250 | 111 | 28 | 0  |

(a) If P = (15, 250) is on the graph of V(t), find the slope of the secant lines PQ when Q is the point (t, V(t)), t = 5, 10, 20, 25, 30.

| $(5,694), m = \frac{694 - 250}{5 - 15} = -44.4$          |
|--|
| $(10, 444), m = \frac{444 - 250}{10 - 15} = -38.8$       |
| $(20, 111), m = \frac{111 - 250}{20 - 15} = -27.8$       |
| $(25,38), m = \frac{38 - 250}{25 - 15} = -22.2$          |
| $(30,0), m = \frac{30 - 250}{0 - 15} = -14.\overline{6}$ |

(b) Estimate the slope of the tangent line at P by averaging the slopes of the two adjacent secant lines.

secant 1: (10, 444) to (15, 250): slope = -38.8secant 2: (20, 111) to (15, 250): slope = -27.8

average = -33.3

- (c) Use a graph to estimate the slope of the tangent line at P.
  - (1) STAT  $\rightarrow$  1:Edit (enter t in  $L_1$ , V in  $L_2$ )
  - (2) 2nd [STAT PLOT] 1:Plot1. ENTER. Choose ON. ENTER.
  - (3) Set window  $[5, 30] \times [0, 694]$ .